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# Liquidity insurance and Pledgeability

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Credit lines (CLs) account for 50-75% of firms' bank financing  
(Greenwald, Krainer, and Paul, 2020)

Typically, they contain:

Covenants on cash holdings/dividends (Sufi, 2009)

Covenants on debt (Acharya, Almeida, Ippolito, Perez, 2020)

CLs often revoked after a covenant violation, esp. to small firms  
(Chodorow-Reich, Darmouni, Luck, and Plosser, 2020)

Current theories don't explain all of these facts

CLs meant to solve low cash problem

But firms need to hold cash to get CLs

CLs should not be revocable to provide liq. insurance

But they are often revoked upon violation of covenants

If CLs need to provide insurance, why revocable?

I.e. why do they have covenants?

Why do they have covenants on cash and leverage?

Why require firm to hoard cash?

Why do firms choose to violate covenants?

Is firm better off losing credit access?

Model a firm's optimal liquidity provision when

Firm subject to random liquidity shock (HT 98)

Pledgeability is limited (HT 98)

Quality of project is not contractable (New)

Benchmarks: Standard contracts don't achieve efficiency

Spot market: not enough debt capacity  $\implies$  underinvestment

CLs: too much insurance  $\implies$  overinvestment

R1: CL with cash covenants achieves efficiency

Liq. insurance creates incentive to continue

Cash covenants solve overinvestment problem

Firm better insured when pledgeability higher

R2: Large firm with multiple projects are better insured

Continuing bad project increases pledgeability

Increasing pledgeability reduces incentive to continue

# BASELINE MODEL

No discounting, universal risk neutrality

Entrepreneur (E) with endowment  $w$

Obtains private benefit  $b$  from not working

Project of quality  $Q \in \{G, B\}$  where  $\Pr(Q = G) = q$

Costs  $I$  at date 0

Needs maintenance cost  $\tilde{\rho} \in \{0, \rho\}$  at date 1 where  $\Pr(\tilde{\rho} = \rho) = \lambda$

Yields  $R$  with proba.  $p_Q$  if E works and  $p_Q - \Delta p$  otherwise

Competitive creditors



Date 0:

E borrows to invest in project

E can sign a contract to mitigate liquidity risk

Date 1:

Liquidity shock  $\tilde{\rho}$  observed

Quality  $Q$  observable but not contractable

E executes contracts: diverts cash/draws down CLs/borrows

Date 2:

E decides whether to exert effort and payoff realized

# Parametric Assumptions

A1. Liquidity shock neither too high nor too low

$$\max \left\{ p_G \left( R - \frac{b}{\Delta p} \right), p_B R \right\} < \rho < p_G R$$

A2. Entrepreneur endowment not too high

$$w \leq I + \lambda q \rho - p_G \left( R - \frac{b}{\Delta p} \right)$$

A3. Bad project is really bad (only for R2b)

$$p_B < p_G - \Delta p$$

If the project is good

$$p_G R > \rho$$

Continue regardless of the liq. shock, conditional on effort

If the project is bad

$$\rho > p_B R > 0$$

Continue only when there is no shock

**B1: EX INTERIM MARKETS  
CANNOT ACHIEVE FIRST  
BEST**

Result: Underinvestment with markets: good projects liquidated

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If  $Q = G$  and  $\tilde{\rho} = \rho$  it's efficient to continue

But to exert effort, E must get  $R_b$  s.t.

$$p_G R_b \geq (p_G - \Delta p) R_b + b \implies R_b \geq \frac{b}{\Delta p}$$

E cannot raise money as creditors cannot break even (by A1)

$$\rho > p_G \left( R - \frac{b}{\Delta p} \right)$$

(Expected) Pledgeability  $\theta := \frac{p_G(R - R_b)}{R} = p_G \left( 1 - \frac{b/R}{\Delta p} \right)$  too low

E can continue project if could borrow against whole cash flow

But E must be compensated to exert effort

E cannot borrow enough to mitigate the liquidity shock

In HT 98, a CL solves the problem: compensate creditors ex ante

Can it solve the problem here, too?

**B2: CREDIT LINE CANNOT  
ACHIEVE FB**



Result: Overinvestment with CL, bad project inefficiently continued

## B2: Credit Line Cannot Achieve FB

Result: Overinvestment with CL, bad project inefficiently continued

Suppose E obtain a CL with limit  $l = \rho$  from creditor

When  $Q = B$ , it is efficient not to continue (by A1)

But E gets paid  $p_B \frac{b}{\Delta p}$  if project continued, and 0 otherwise

CLs provide liquidity insurance when firm cannot borrow

Good project efficiently continued

CLs also provide liquidity insurance when firm shouldn't continue

Bad project inefficiently continued

E doesn't have skin in the game: cost entirely borne by creditor

**R1: CREDIT LINE WITH  
CASH COVENANTS  
ACHIEVES FB**

# CL drawdowns are harder to divert

E can divert its own cash but not CL drawdowns

Use of proceeds often restricted

E.g. Revolving Credit Facility Agreement (NORDSTROM)

**Section 2.3. Use of Proceeds.** *The proceeds of the Loans shall be used by the Borrower only for working capital, capital expenditures and other lawful general corporate purposes of the Borrower and its Subsidiaries, including (a) loans made by the Borrower to its Subsidiaries and (b) the payment of commercial paper ... the proceeds of the Loans shall not be used to finance any acquisition ...*

**Section 6.2. Restricted Payments.** *The Borrower shall not, and shall not permit any Subsidiary to, declare, pay or make, or agree to declare, pay or make, any Restricted Payment... (“Restricted Payment” means (i) any dividend or other distribution ...)*

# R1: CL with Cash Covenants Achieves FB

Suppose E has cash  $c = p_B \frac{b}{\Delta p}$  and CL  $l = \rho - c$  with cash covenants

When  $Q = B, \tilde{\rho} = \rho$ , E diverts cash

$$c \geq p_B \frac{b}{\Delta p}$$

When  $Q = G, \tilde{\rho} = \rho$ , E does not divert cash

$$c < p_G \frac{b}{\Delta p}$$

When  $\tilde{\rho} = 0$ , firm always diverts cash, but project continued

# Pledgeability vs Liquidity Insurance

Without liquidity insurance:

Low pledge.  $\Rightarrow$  Too little debt capacity  $\Rightarrow$  Underinvest (HT 98)

With (too much) liquidity insurance:

Low pledge.  $\Rightarrow$  Too little skin in the game  $\Rightarrow$  Overinvest (New)

Covenants on cash solve the problem: insurance not too much

E better insured when pledgeability higher

Firm cash holdings drop after CL drawdown

Direct evidence (Berrospide and Meisenzahl, 2015)

*“... a one standard deviation increase in drawdowns reduces average cash holdings by about 1 percent of total assets...reduce cash holdings by about 8 percent...”*



# Large Firms

In this section, we model a firm with two projects

i.i.d. quality shocks

perfectly correlated liquidity shocks

Firm can decide to continue each project *independently*

Each project has its own private benefit  $b$

Without liquidity shock: all projects should be continued

With liquidity shock: only good project(s) should be continued

# R2A: MULTIPLE PROJECTS INCREASE PLEDGEABILITY

Result: Pledgeability higher with two projects (Laux 01)

$$p_A p_B R_b \geq (p_A - \Delta p)(p_B - \Delta p)R_b + 2b$$

In expectation, E gets lower than two separate projects

$$p_A p_B R_b = \frac{2b}{1 - \frac{p_A - \Delta p}{p_A} \frac{p_B - \Delta p}{p_B}} < p_A \frac{b}{\Delta p} + p_B \frac{b}{\Delta p}$$

E's rent is at least  $R_b$  to induce him to exert effort

Would like to punish E in case of failure to reduce rent

Impossible with only one project because of limited liability

But possible with two projects if not continued independently

If Project 1 fails, with prob  $p_H$  other succeeds and E gets  $R_b$

Even under LL, E's income on Project 1 can be reduced to  $-R_b$

# R2B: FIRM BETTER INSURED WITH MULTIPLE PROJECTS

## R2b: E Better Insured with Multiple Projects

Result: E only continues good project 2 even fully insured (New)



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Suppose both projects shocked and project 1 is good

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## R2b: E Better Insured with Multiple Projects

Result: E only continues good project 2 even fully insured (New)

Suppose both projects shocked and project 1 is good

E chooses whether to continue project 2 at date 1

Continuing project 2 increases private benefit by  $b$

E needs to be compensated for effort more

Continuing project 2 increases pledgeability

E extracts fewer rents from the good project 1

Good project 2 increases expected compensation for effort more

E relatively more inclined to continue

$$\underbrace{\frac{2b}{1 - \frac{p_G - \Delta p}{p_G} \frac{p_G - \Delta p}{p_G}}}_{\text{Continue both G \& G}} \geq \underbrace{\frac{b}{1 - \frac{p_G - \Delta p}{p_G}}}_{\text{Continue only G}}$$

Bad project 2 dilutes rent from the good project 1 more

E more incentivized not to continue

$$\underbrace{\frac{b}{1 - \frac{p_G - \Delta p}{p_G}}}_{\text{Continue only G}} \geq \underbrace{\frac{2b}{1 - \frac{p_A - \Delta p}{p_A} \frac{p_B - \Delta p}{p_B}}}_{\text{Continue both G \& B}} \Leftrightarrow \Delta p \leq p_G - p_B \quad (\text{A3})$$

Good project 2 increases expected compensation for effort more

E relatively more inclined to continue

Bad project 2 dilutes rent from the good project 1 more

E more incentivized not to continue

E only continues an additional project B if it's good (by A3)

E can be better insured with two projects

Firm lacks pledgeability to borrow when liquidity shock occurs

CLs provide liq. insurance to continue efficient project

Liquidity insurance creates incentive to continue inefficiently

Covenants on cash require firm to have skin in the game

Firm better insured when pledgeability higher

Continuing inefficient project increases pledgeability

Large firms can be better insured

THANK YOU!

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